### REVIEW PAPER

### THE ROLE OF ALPHA PARTICLES IN TOKAMAK REACTORS

Ya.I. KOLESNICHENKO
Institute for Nuclear Research of the
Ukrainian SSR Academicy of Sciences,
Kiev, Union of Soviet Socialist Republics

ABSTRACT. The author reviews the theoretical work on those properties of a thermonuclear plasma that relate to the charged products of nuclear fusion reactions  $-\alpha$ -particles. Three basic lines of research - on classical mechanisms of  $\alpha$ -particle loss in tokamaks, collective processes in the plasma initiated by  $\alpha$ -particles, and the energy balance stability of a thermonuclear plasma - are considered.

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#### 1. INTRODUCTION

In recent years considerable progress has been made in plasma experiments and in our understanding of the physics of a high-temperature plasma. The most striking progress has been made with tokamak-type devices. As a result, thermonuclear research programmes have been set up in a number of countries which aim at conducting demonstration fusion reactor experiments on tokamaks in the period 1980–90 [1–3, 125]. This has made it necessary to solve a new set of physics and engineering problems, which in turn has stimulated

$$\frac{a_{\rm eff}}{r_{\rm B\alpha}} < \left(\frac{v_{\alpha}}{v_{\alpha} - v_{1}}\right)^{1/2} \left(\omega_{\rm B\alpha} \tau_{\rm f}\right)^{1/4} \frac{v_{\rm Ti}}{v_{\alpha}} \tag{148}$$

When this inequality holds the confinement time of resonance  $\alpha$ -particles in the plasma is short:  $\tau_{n\alpha} < \tau_{\parallel}^{\alpha e}$ . In the opposite case,  $\tau_{n\alpha} > \tau_{\parallel}^{\alpha e}$ , and the instability in question is suppressed by Coulomb collisions after a time of the order of  $\tau_{\parallel}^{\alpha e}$ .

The foregoing evaluations for turbulent particle fluxes, together with condition (148), remain valid to within a factor of the order of  $\sqrt{\beta}$  if the non-linear mechanism leading to energy transfer into the damped part of the spectrum consists of three-plasmon processes involving compressional Alfvén waves (under tokamak-reactor conditions, processes involving slow magnetoacoustic waves are impossible).

In conclusion, let us compare the turbulent electron and ion fluxes obtained with the neoclassical fluxes ( $\Gamma^N$ ). We find that  $\Gamma^T > \Gamma^N$  for the typical parameters of tokamak reactors. As a result, the turbulent state discussed here may be accompanied by ion diffusion towards the axis of the plasma column.

# 3.4.3. The Sigmar-Chan theory of α-particle diffusion induced by an Alfvén instability due to trapped particles [74]

Let us consider the possibility of anomalous diffusion of  $\alpha$ -particles, assuming that these particles excite an instability characterized by the conditions  $\xi_p \ll 1$ ,  $\eta_p \gtrsim 1$ ,  $k_p^2 \gg k_b^2$  (see Section 3.3.1.2).

To carry out this analysis we shall need to know the threshold density for the instability  $(n_{\alpha}^{cr})$ . Following Sigmar and Chan [74], we shall consider it to be determined by the collisional energy dissipation of waves on trapped electrons, and we shall not take into account quasi-linear distortion of the electron distribution function. Thus, the system of equations describing the development of the instability consists of only two equations: a quasi-linear equation for the  $\alpha$ -particle distribution function and an equation for the waves. The system can be written in the following form [74]:

$$\frac{\partial f_{\alpha}}{\partial t} = \frac{\partial}{\partial \mathscr{E}} D_{\varepsilon\varepsilon} \frac{\partial f_{\alpha}}{\partial \mathscr{E}} - \frac{D_{\rho\rho}}{d^2(t)} f_{\alpha} + St^{coll} \{f_{\alpha}\}$$

$$+\frac{n\delta(v-v_{\alpha})}{\tau_{f}^{4\pi}v_{\alpha}^{2}}\tag{149}$$

$$\frac{\partial E_{\vec{k}}}{\partial t} = \gamma_{\vec{k}} \vec{E}_{\vec{k}}$$
 (150)

Here, d(t) is the characteristic radial dimension of the inhomogeneity of the  $\alpha$ -particle distribution,  $\mathscr{E}=v^2/2$ , and the diffusion coefficients  $D_{\epsilon\epsilon}$  and  $D_{\rho\rho}$  are given by the expressions:

$$D_{\epsilon\epsilon} = \sum_{\vec{k}} |E_{\rho\vec{k}}|^2 \sum_{\rho} \frac{|P|}{k_{\rho}^2} J_{\rho}^2 (\eta_{\rho}^{\nu}) \frac{2\pi\sqrt{\epsilon} e^2}{qR\sqrt{\mathscr{E}}m^2}$$
 (151)

$$D_{\rho\rho} = \frac{c^2}{B^2} \sum_{\vec{k}} |E_{\theta\vec{k}}|^2 \sum_{\rho} \frac{8\sqrt{2\pi^2}}{|\rho|} Rq J_{\rho}^2(\eta_{\rho}^{\nu}) \quad (152)$$

in which  $\eta_{\rho}^{\rm V}$  is identical with  $\eta_{\rho}$  as determined by Eq.(88) if we put  ${\rm v}_{\alpha}={\rm v}$  in the latter. The diffusion coefficient  ${\rm D}_{\rho\rho}$  is obtained from the equation

$$D_{\rho\rho} = \int_{-\infty}^{t} dt' \left\langle \frac{dr_{GC}(t)}{dt} \frac{dr_{GC}(t')}{dt'} \right\rangle$$
 (153)

where  $dr_{GC}/dt = c\widetilde{E}_{\theta}/B$ , and () indicate averaging overall the phase angles between the waves and particles. The dependence d(t) is determined by the particle conservation equation which follows from Eq.(149):

$$\frac{\partial n_{\alpha}}{\partial t} - \frac{1}{\rho} \frac{\partial}{\partial \rho} r \overline{D}_{\rho \rho} \frac{\partial n_{\alpha}}{\partial \rho} = \frac{n}{\tau_{f}}$$
 (154)

where

$$\overline{D}_{\rho\rho} = 2\sqrt{2\pi}J_{\rho}^{2}(\eta_{\rho})\frac{c^{2}|E_{\theta}|^{2}}{B^{2}}\frac{\sqrt{\epsilon}}{|\rho|\omega_{b\alpha}}$$
(155)

Note that the diffusion coefficient  $\overline{D_{\rho\rho}}$  is easy to obtain by means of the expression

$$\Gamma_{\alpha} = -\frac{2c}{e_{\alpha}B} \int \frac{d\vec{k}}{(2\pi)^3} k_b (N_{\vec{k}} \delta \gamma_{\vec{k}\alpha} + \gamma_{\vec{k}\alpha} \delta N_{\vec{k}})$$
(156)

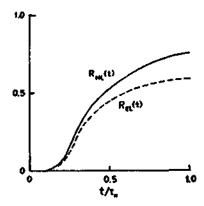


FIG. 19. Alpha-particle loss rate coefficient,  $R_{\rm NL}$ , and  $\alpha$ -particle energy loss rate coefficient,  $R_{\rm EL}$ , as a function of time.  $R_{\rm NL}$  and  $R_{\rm EL}$  are determined by Eq.(158) [74].

if we allow for the fact that

$$\delta \gamma_{\alpha} = \sum_{\rho} \pi \epsilon \frac{m_{\alpha}}{m_{i}} \frac{\omega_{B\alpha}}{\omega} \frac{k_{b}}{k_{\rho}^{2} qR} |\rho| v_{\alpha} J_{\rho}^{2} (\eta_{\rho}) \frac{1}{n_{i}} \frac{\partial n_{\alpha}}{\partial \rho}$$

(157)

$$E_{\theta}/E_{\rho} = k_{b}/k_{\rho}$$

and put  $\delta N_{\vec{k}} = 0$ . In fact, as can be seen from expressions (135), the correction  $\delta N_{\vec{k}}$  plays an important role. Nevertheless, in a qualitative description of diffusion, it is possible to use the expression for  $\overline{D_{\rho\rho}}$  (155), which does not take this correction into account.

This system of equations was solved numerically in Ref.[74]. The following tokamak parameters were used: B = 50 kG, a/R = 120/400, q(a) = 2.5,  $n_e = 5 \times 10^{13} \text{ cm}^{-3}$ , T = 15 keV, and I = 3.6 MA. It was assumed that the instability develops on the second bounce harmonic.

The calculations showed that turbulent loss of  $\alpha$ -particles is sufficiently rapid for a distribution  $f_{\alpha}(\epsilon,t)$  with  $t \sim \tau_{\parallel}^{\alpha e}$ ,  $\mathcal{E} \lesssim \mathcal{E}_{\alpha}$  to have a maximum. This means that there is a steady turbulent state for  $t \gtrsim \tau_{\parallel}^{\alpha e}$ . The amplitudes of the electromagnetic fields in this state reach values of  $E^2/(8\pi nT) \simeq 10^{-5}$ . It should be noted, however, that they correspond to a very high noise energy:  $W/(nT) = 1.8 \times 10^{-2} (10^9/v_A)^2$ . At this energy a strong interaction between waves is to be expected which is not taken into account by Eq.(150).

To illustrate the dynamics of the development of the instability and its influence on  $\alpha$ -particle losses, Fig.19 shows the dependence on time of the  $\alpha$ -particle loss rate coefficient,  $R_{NL}$ , and the  $\alpha$ -particle energy loss rate coefficient,  $R_{EL}$ , which were obtained as follows by the authors of Ref.[74]:

$$R_{NL} = 1 - n_{\alpha}(t)/(nt/\tau_f)$$

$$R_{EI} = \Delta (n_{\alpha} \ell_{\alpha})/(\ell_{\alpha} nt/\tau_f)$$
(158)

where

$$\Delta (n_{\alpha} \mathcal{O}_{\alpha}) = \int_{0}^{t} dt \, d^{-2}(t) \int d\vec{v} \, \frac{mv^{2}}{2} \, D_{\rho\rho} \, f_{\alpha}$$

# 3.5. Alpha-particle losses in tokamaks as a result of the development of thermonuclear cone instabilities [38]

Turbulent diffusion across the magnetic field is not the only cause of anomalous  $\alpha$ -particle losses in tokamaks. A simpler mechanism — diffusion in velocity space — can also lead to such losses if conetype thermonuclear instabilities are excited in the plasma. Let us take a closer look at the effectiveness of this leakage channel for fast ions.

It is clear that the number of  $\alpha$ -particles entering the loss region as a result of quasi-linear diffusion is strongly dependent on the width of the region of resonance interaction between  $\alpha$ -particles and waves  $(\Delta v_1^r)$ . When the instability first arises this region is very narrow,  $\Delta v_1^r \sim v_{T\Sigma} \chi_s$ , but it can become considerably wider as the instability develops. The broadening is accompanied by a reduction in the gradients of the function  $f(\vec{v})$  and consequently by a decrease in the growth rate of the instability. It can therefore lead to the establishment of some steady state in which  $0 < \gamma_{\alpha}^{st} < \gamma_{\alpha}$  (t = 0), the growth rate being non-zero because of the systematic influx into the resonance region of  $\alpha$ -particles produced by the thermonuclear reaction.

The quasi-linear evolution of the  $\alpha$ -particle distribution begins at the time when  $n_{\alpha} \approx n_{\alpha}^{cr}$  and in some wave vector range  $\gamma_{\vec{k}} \cong 0$ . For the instabilities discussed in Section 3.3.3,  $\gamma_{\vec{k}} \approx 0$  if  $\gamma_{\vec{k},\alpha} \approx \omega_{b\alpha}$ , i.e. the vanishing of the growth rate is not due to the background plasma. As a result, the time for establish-

- [57] KALADZE, T.D., LOMINADZE, D.G., STEPANOV, K.N., Zh. Tekh. Fiz. 44 (1974) 273 (Sov. Phys. – Tech. Phys. 19 (1974) 175).
- [58] KALADZE, T.D., LOMINADZE, D.G., STEPANOV, K.N., in Controlled Fusion and Plasma Physics (Proc. 6th Europ. Conf. Moscow, 1973) Vol.1, Moscow (1973) 646.
- [59] BELIKOV, V.S., KOLESNICHENKO, Ya.I., ORAEVSKIJ, V.N., Zh. Ehksp. Teor. Fiz. 66 (1974) 1686 (Sov. Phys. – JETP 39 (1974) 828).
- [60] BELIKOV, V.S., KOLESNICHENKO, Ya.I., Zh. Tekh. Fiz. 45 (1975) 1798 (Sov. Phys. - Tech. Phys. 20 (1976) 1146.
- [61] MIKHAJLOVSKIJ, A.B., Zh. Ehksp. Teor. Fiz. 68 (1975) 1772 (Sov. Phys. – JETP 41 (1975) 890).
  - [62] LOMINADZE, D.G., MIKHAJLOVSKIJ, A.B., Fiz. Plazmy 1 (1975) 520 (Sov. J. Plasma Phys. 1 (1975) 291).
  - [63] MAI, L.P., HORTON, W., Phys. Fluids 18 (1975) 356.
  - [64] BELIKOV, V.S., KOLESNICHENKO, Ya.I., ORAEVSKIJ, V.N., in Problemy Teorii Plazmy (Problems of Plasma Theory), Naukova Dumka, Kiev (1976) 56.
  - [65] KALADZE, T.D., LOMINADZE, D.G., STEPANOV, K.N., in Voprosy Atomnoj Nauki Tekhniki (Problems of Atomic Science and Technology) Vol.1, Khar'kov (1976) 5.
  - [66] BEASLEY, C.O., LOMINADZE, D.G., MIKHAJLOVSKIJ, A.G., Fiz. Plazmy 2 (1976) 170 (Sov. J. Plasma Phys. 2 (1976) 95).
  - [67] KALADZE, T.D., LOMINADZE, D.G., MIKHAILOVSKIJ, A.B., POKHOTELOV, O.A., Nucl. Fusion 16 (1976) 465.
  - [68] KALADZE, T.D., MIKHAILOVSKIJ, A.B., Nucl. Fusion 17 (1977) 411.
  - [69] BELIKOV, V.S., KOLESNICHENKO, Ya.I., MIKHAILOVSKIJ, A.G., YAVORSKIJ, V.A., Fiz. Plazmy 3 (1977) 263 (Sov. J. Plasma Phys. 3 (1977).
  - [70] KALADZE, T.D., MIKHAILOVSKIJ, A.B., Nucl. Fusion 17 (1977) 729.
- [71] MIKHAJLOVSKIJ, A.B., FRENKEL', A.L., Fiz. Plazmy
   3 (1977) 1219 (Sov. J. Plasma Phys. 3 (1977) 677).
  - [72] SIGMAR, D.J., CHAN, H.C., in Controlled Fusion and Plasma Physics (Proc. 8th Europ. Conf. 1977) Vol.1 (1977) 167.
- [73] BELIKOV, V.S., KOLESNICHENKO, Ya.I., in Controlled Fusion and Plasma Physics (Proc. 8th Europ. Conf. 1977) Vol.2 (1977) 243.
- [74] SIGMAR, D.J., CHAN, H.C., Nucl. Fusion 18 (1978) 1569.
- [75] SHAFRANOV, V.D., in Voprosy Teorii Plazmy Vol.3, Moscow (1963) 3 (Problems of Plasma Physics Vol.3, Consultants Bureau, N.Y. (1967) 1).
- [76] MIKHAJLOVSKIJ, A.B., in Voprosy Teorii Plazmy,3, Moscow (1963) 141 (Problems of Plasma Physics, Vol.3, Consultants Bureau, N.Y. (1967) 159).
- [77] AKHIEZER, A.I., AKHIEZER, I.A., POLOVIN, R.V., SITENKO, A.G., STEPANOV, K.N., Ehlektrodinamika Plazmy (Plasma Electrodynamics), Moscow (1974).
- [78] KADOMTSEV, B.B., POGUTSE, O.P., in Plasma Physics and Controlled Nuclear Fusion Research (Proc. 3rd Int. Conf. Novosibirsk, 1968) Vol.2, IAEA, Vienna (1969) 125.
- [79] TIMOFEEV, A.V., Fiz. Plazmy 2 (1976) 419 (Sov. J. Plasma Phys. 2 (1977) 280).
- [80] KADOMTSEV, B.B., Kollektivnye yavleniya v plazme (Collective Phenomena in a Plasma), Nauka, Moscow (1976).

- [81] MILLS, R.G., The Problem of Control of a Thermonuclear Reactor, Proc. Symp. Los Alamos Sci. Lab. Report LA-4250 (1969).
- [82] GOLOVIN, I.N., DNESTROVSKY, Yu.N., KOSTOMAROV, D.P., Tokamak as a Possible Fusion Reactor - Comparison with Other CTR Devices, Proc. Nucl. Fus. Reactor Conf. (Culham, 1969) 194.
- [83] KOLESNICHENKO, Ya.I., At. Ehnerg. 31 (1971) 295.
- [84] VAN'T-HOFF, Etudes de dynamique chimique (Studies of Chemical Dynamics), Amsterdam (1884).
- [85] SEMENOV, N.N., Tsepnye reaktsii (Chain Reactions), Goskhimizdat, Moscow (1934).
- [86] FRANK-KAMENETSKIJ, D.A.. Diffuziya i teploperedacha v khimicheskoj kinetike (Diffusion and Heat Transfer in Chemical Kinetics), USSR, Academy of Sciences Press, Moscow (1947).
- [87] MILLS, R.G., Time-dependent Behaviour of a Fusion Reactor. Preprint MATT-728 (1970).
- [88] OHTA, M., YAMATO, H., MOR!, S., in Plasma Physics and Controlled Nuclear Fusion Research, (Proc. 4th Int. Conf. Madison, 1971) Vol.3, IAEA, Vienna (1971) 423.
- [89] POWELL, C., HAHN, O.J., Nucl. Fusion 12 (1972) 667.
- [90] KOLESNICHENKO, Ya.I., Nucl. Fusion 12 (1972) 419.
- [91] NASTOYASHCHIJ, A.F., At. Ehnerg. 32 (1972) 43.
- [92] OHTA, M., YAMATO, H., MORI, S., Nucl. Fusion 12 (1972) 604.
- [93] KOLESNICHENKO, Ya.I., REZNIK, S.N., Nucl. Fusion 13 (1973) 167.
- [94] OHTA, M., YAMATO, H., MORI, S., J. Nucl. Sci. Technol. (Japan) 10 (1973) 353.
- [95] OHNISHI, M., YOSHIKAWA, H., WAKABAYASHI, I., Nucl. Fusion 13 (1973) 761.
- [96] STACEY, W.M., Nucl. Fusion 13 (1973) 843.
- [97] FUJISAWA, T., Nucl. Fusion 14 (1974) 173.
- [98] COHN, R.W., EMMERT, G.A., Nucl. Fusion 14 (1974)
- [99] STACEY, W.M., Nucl. Fusion 15 (1975) 63.
- [100] KOLESNICHENKO, Ya.I., REZNIK, S.N., YAVORSKIJ, V.A., in Controlled Fusion and Plasma Physics (Proc. 7th Europ. Conf. Lausanne, 1975) Vol.1 (1975) 23.
- [101] KCLESNICHENKO, Ya.I., REZNIK, S.N., YAVORSKIJ, V.A., Nucl. Fusion 16 (1976) 105.
- [102] KGLESNICHENKO, Ya.I., REZNIK, S.N., FURSA, A.D., Fiz. Plazmy 2 (1976) 905 (Sov. J. Plasma Phys. 2 (1976) 502).
- [103] LADIKOV, Yu.P., PAGUTA, M.T., Ukr. Fiz. Zh. 21 (1976) 1288.
- [104] SAITO, H., KATSURAI, M., TSYJI, H., SEKIGUCHI, T., in Plasma Physics and Controlled Nuclear Fusion Research (Proc. 6th Int. Conf. Berchtesgaden, 1976) Vol.3, IAEA, Vienna (1977) 337.
- [105] KOLESNICHENKO, Ya.I., REZNIK, S.M., ibid., 347.
- [106] VOLKOV, T.F., IGITKHANOV, Yu.L., TOKAR, M.Z., ibid., 359.
- [107] REZNIK, S.N., The Instability of Energy Balance and Number of Particles in a Thermonuclear Plasma, Kiev Institute of Nuclear Research Preprint KIYal-20-77 (1977).
- [108] KOLESNICHENKO, Ya.I., REZNIK, S.N., Nucl. Fusion 18 (1978) 1535.